
Lectures: Condensed Matter II

1 – Quantum dots

2 – Kondo effect: Intro/theory.

 3 – Kondo effect in nanostructures

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Lecture 3: Outline

- Quantum Dots: brief review.
 - Kondo effect: Review.
 - Kondo effect in quantum dots.
 - Kondo effect in Single Molecule Transistors.
 - Kondo effect in Surfaces (STM, “quantum mirage”).
 - Kondo effect in carbon nanotubes.
-

History of Kondo Phenomena

- Observed in the '30s
- Explained in the '60s
- Numerically Calculated in the '70s (NRG)
- Exactly solved in the '80s (Bethe-Ansatz)

So, what's new about it?

Kondo correlations observed in many different set ups:

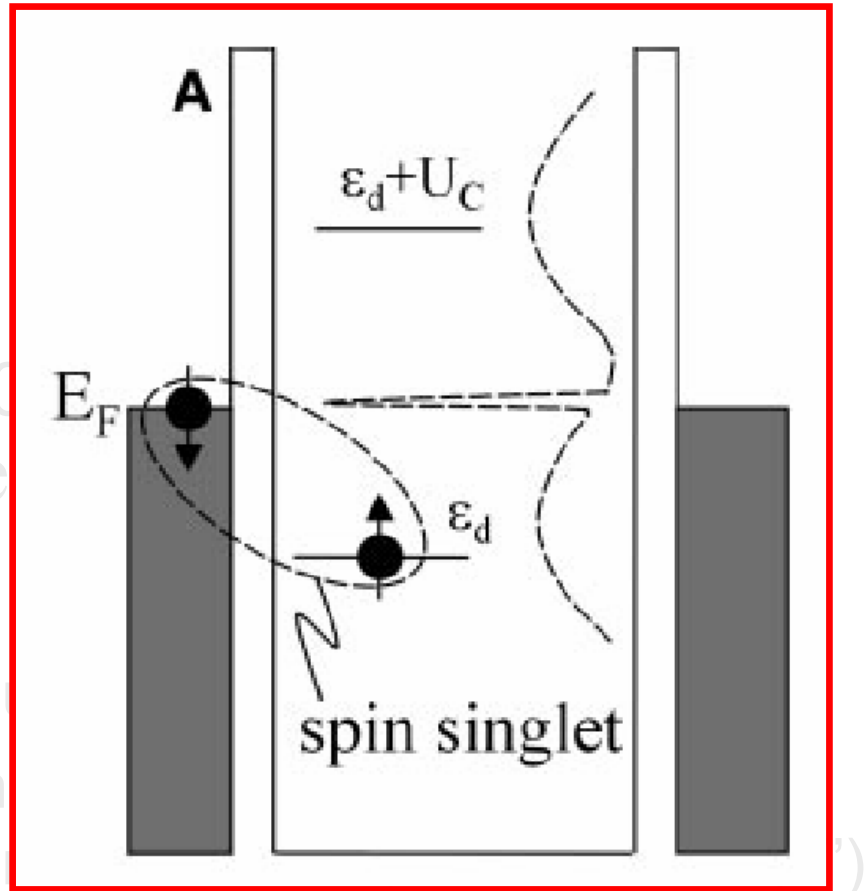
- Transport in quantum dots, quantum wires, etc
 - STM measurements of magnetic structures on metallic surfaces (e.g., single atoms, molecules. “Quantum mirage”)
 - ...
-

History of Kondo Phenomena

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 - Explained in the '60s
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- So, what's new?

Kondo correlations observed

- Transport in quantum dots, q
- STM measurements of magn surfaces (e.g., single atoms,
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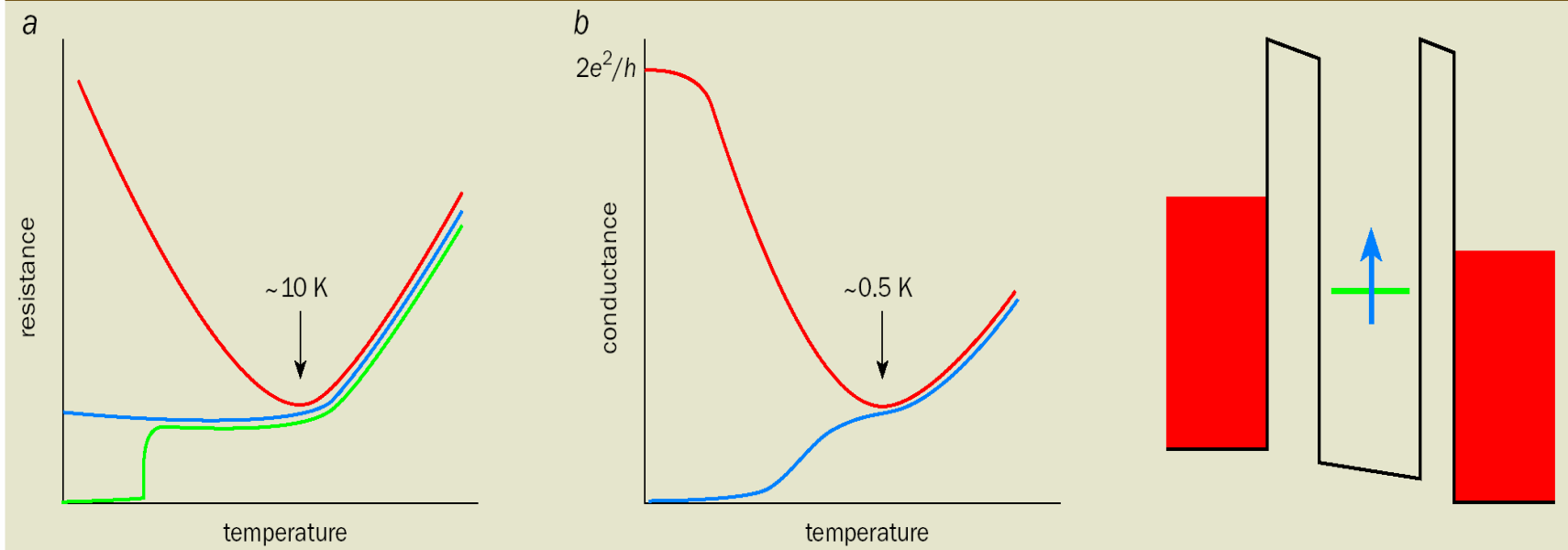
Kondo Effect in Quantum Dots

Revival of the Kondo effect

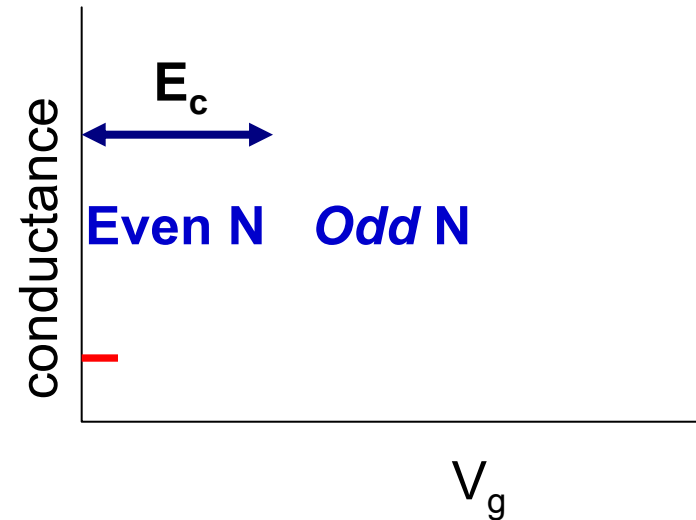
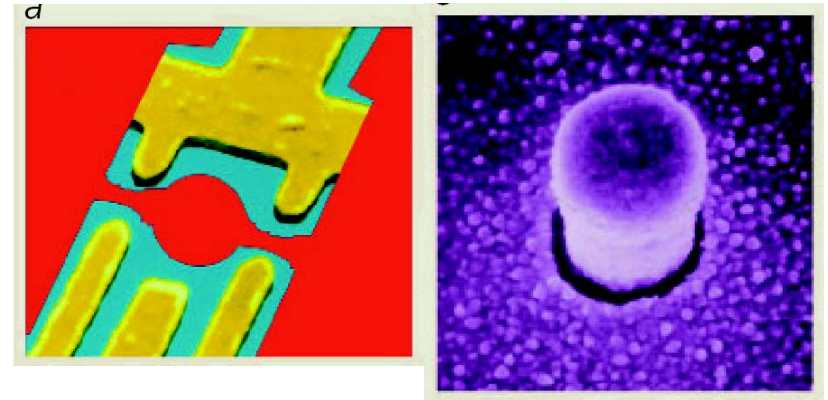
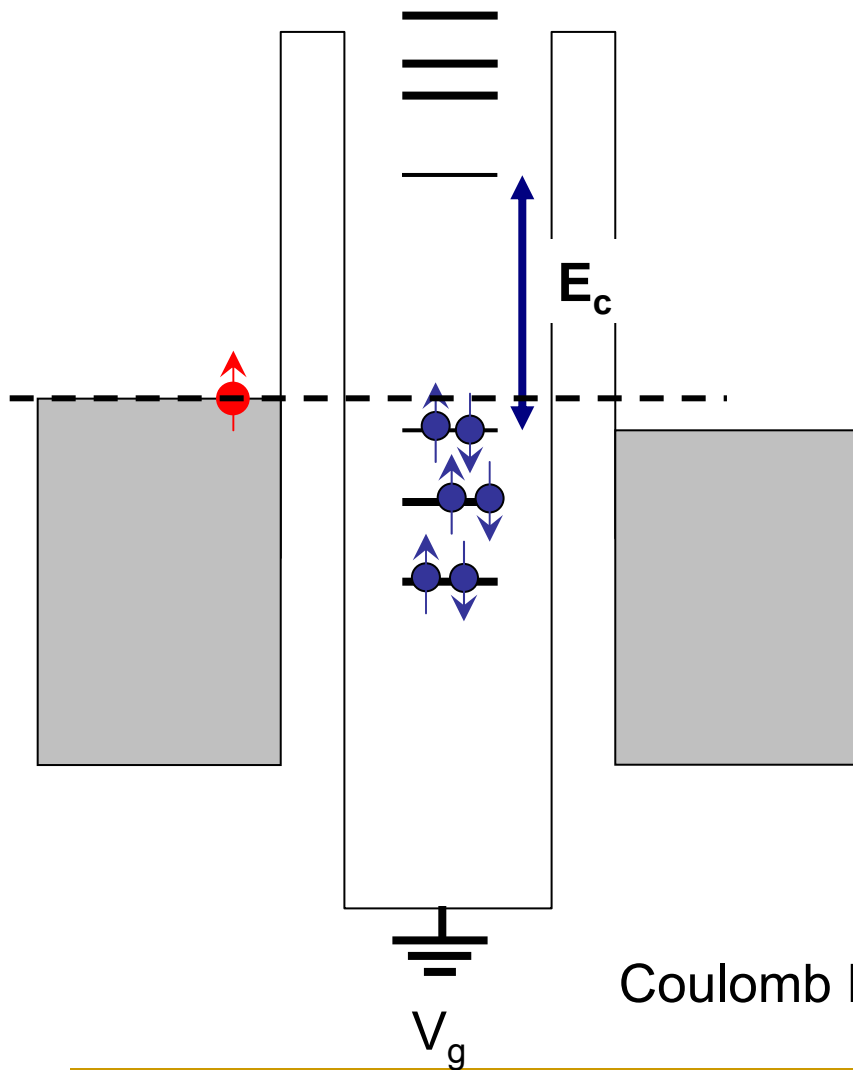


Leo Kouwenhoven and Leonid Glazman

1 The Kondo effect in metals and in quantum dots

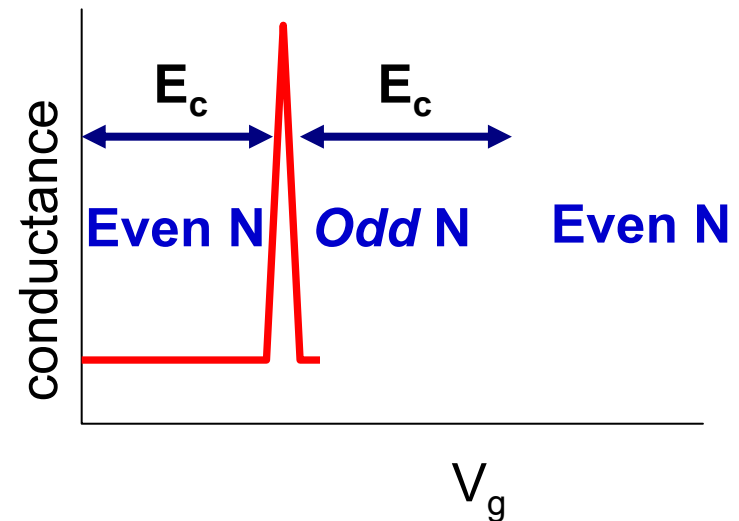
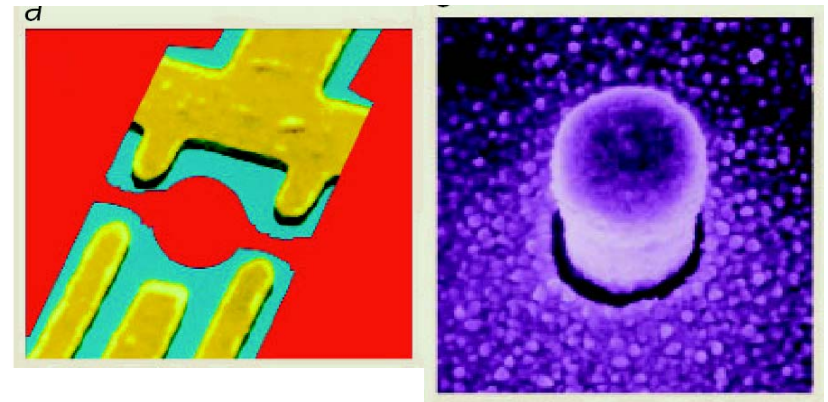
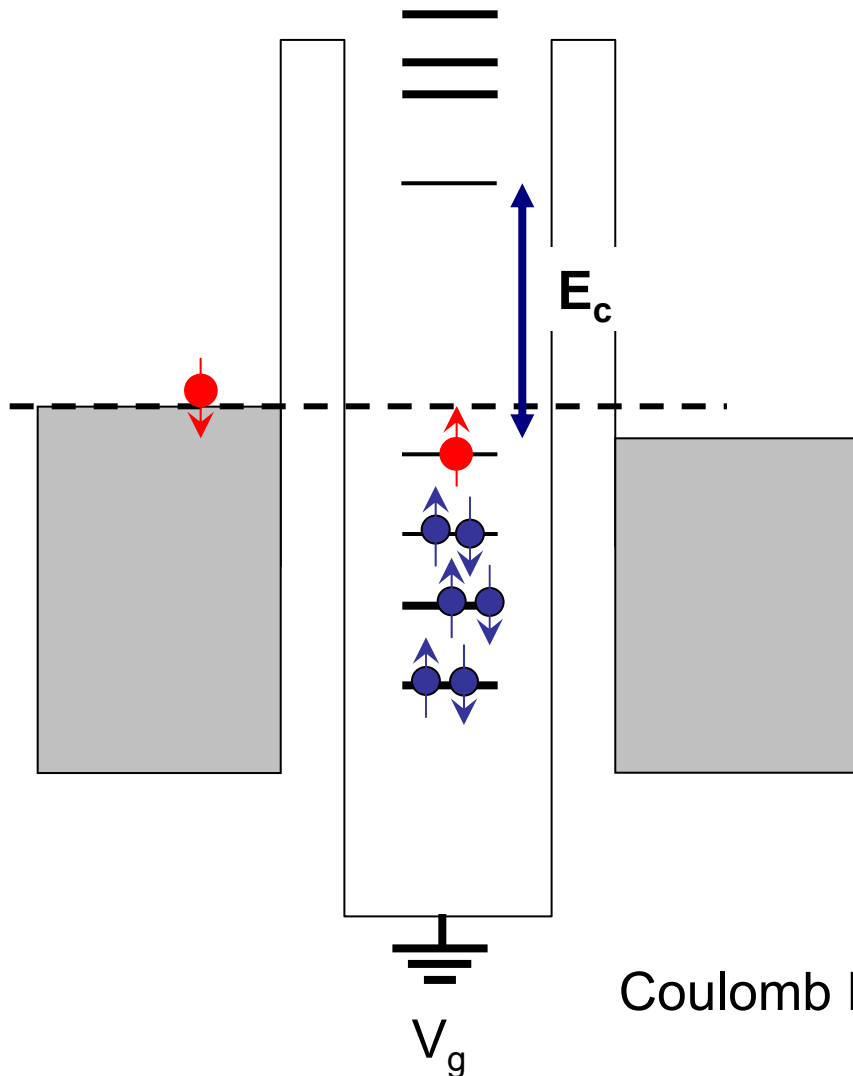


Coulomb Blockade in Quantum Dots



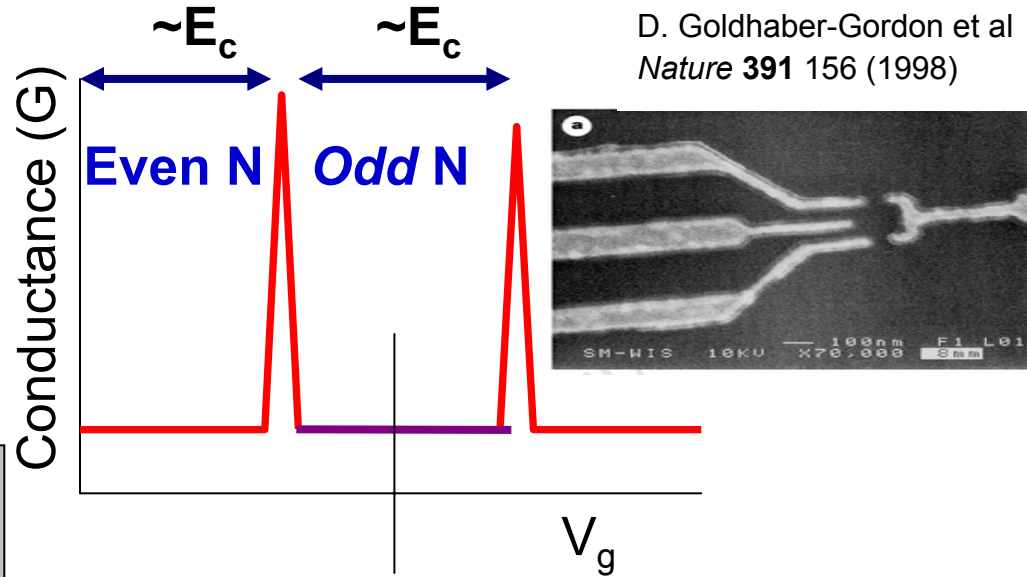
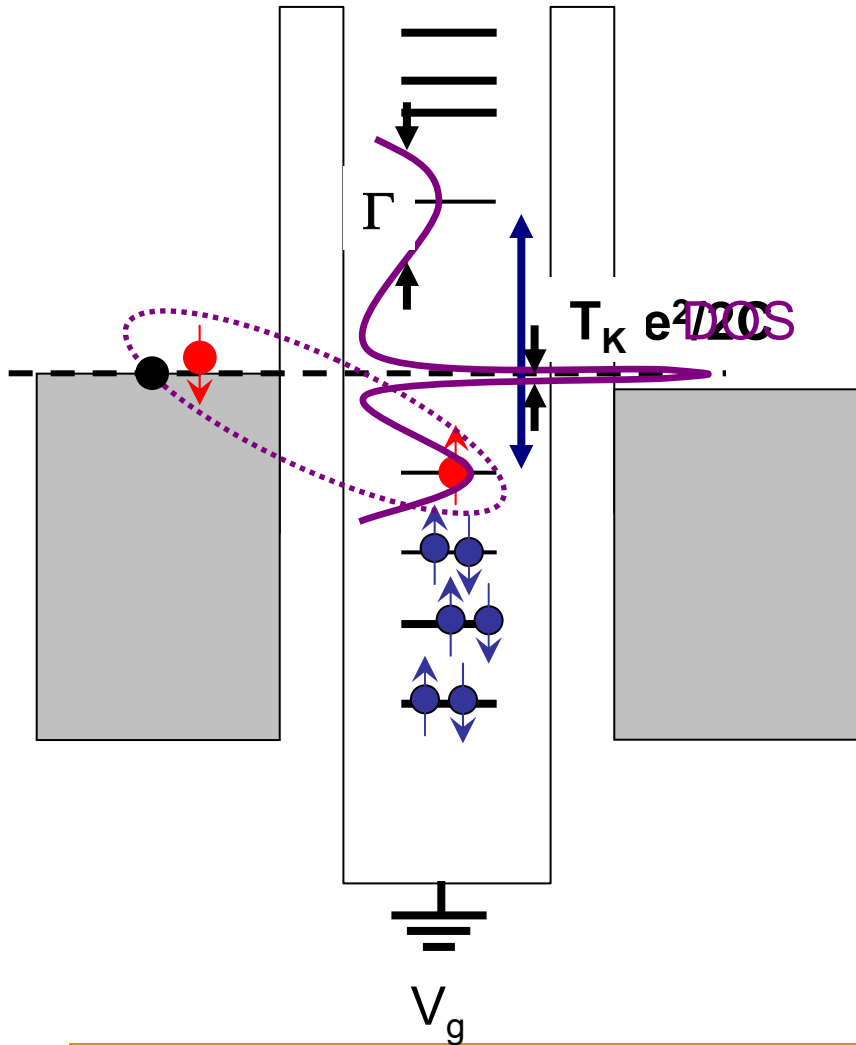
Coulomb Blockade in Quantum Dots

Coulomb Blockade in Quantum Dots



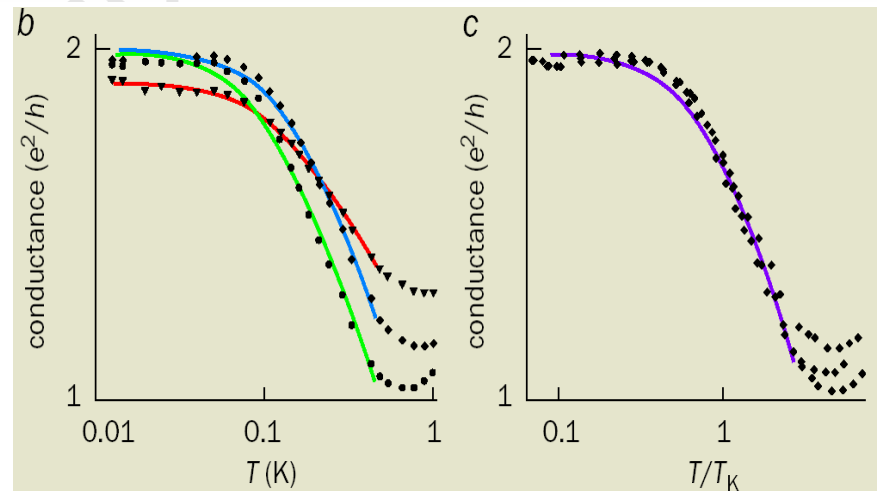
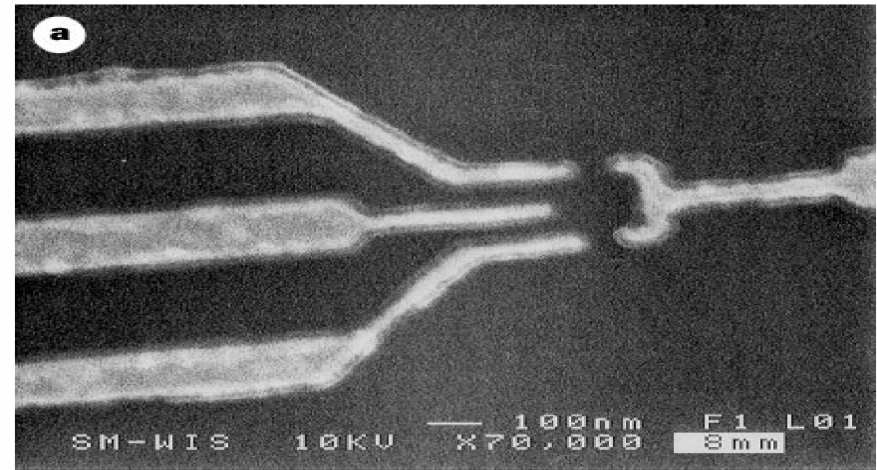
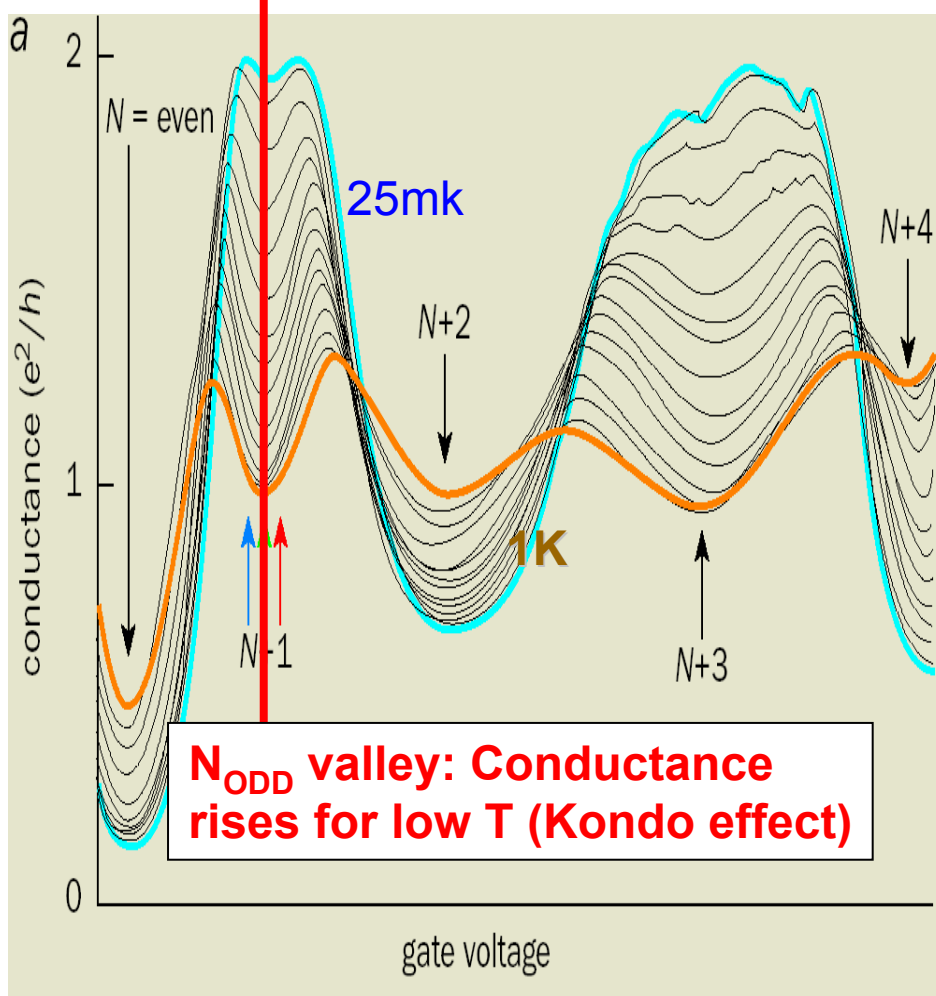
Coulomb Blockade in Quantum Dots

Kondo Effect in Quantum Dots



- $T > T_K$: Coulomb blockade (**low G**)
- $T < T_K$: Kondo singlet formation
- **Kondo resonance** at E_F (width T_K).
- New conduction channel at E_F :
Zero-bias enhancement of G

Kondo Effect in CB-QDs



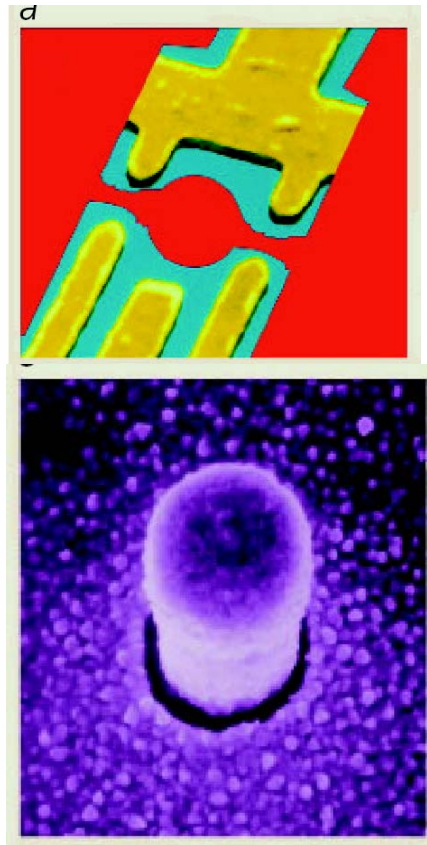
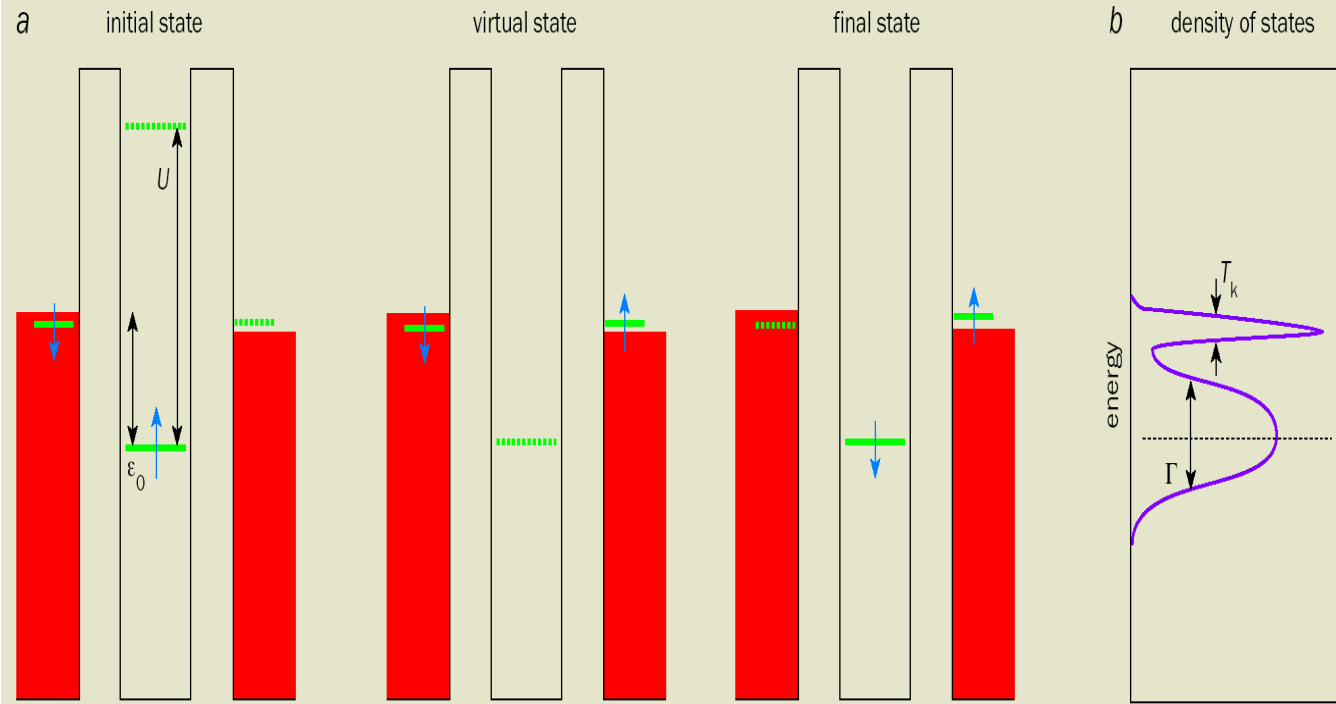
Kondo Temperature T_K : only scaling parameter ($\sim 0.5\text{K}$, depends on V_g)

Kowenhoven and Glazman *Physics World* – Jan. 2001.

From: Goldhaber-Gordon *et al. Nature* **391** 156 (1998)

Kondo Effect in Quantum Dots

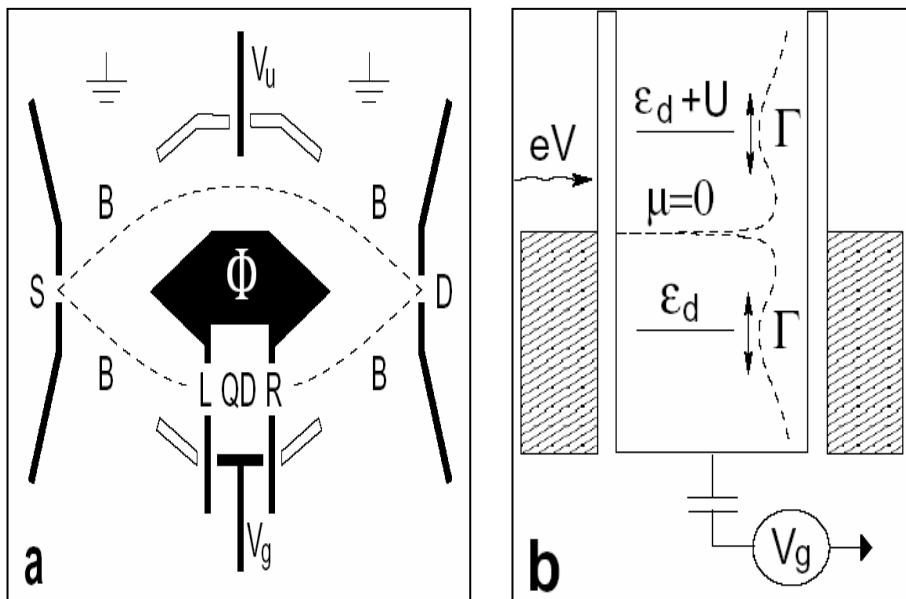
2 Spin flips



Basic mechanism of the Kondo effect in
Coulomb Blocked quantum dots

Theory-Experiment ballgame

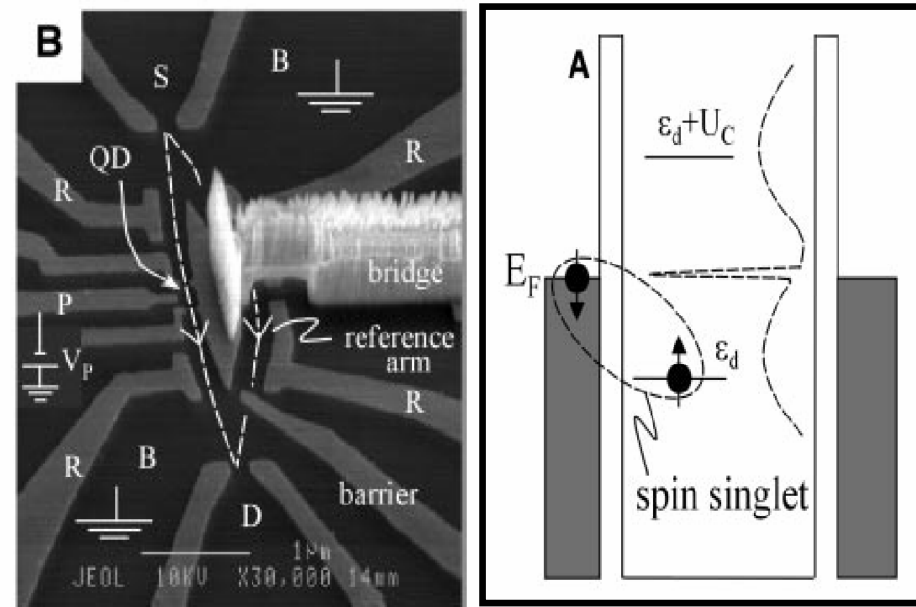
Transmission Phase Shift of a Quantum Dot with Kondo Correlations



Theory

(Gerland et al.
PRL **84** 3710 (2000))

Phase Evolution in a Kondo-Correlated System

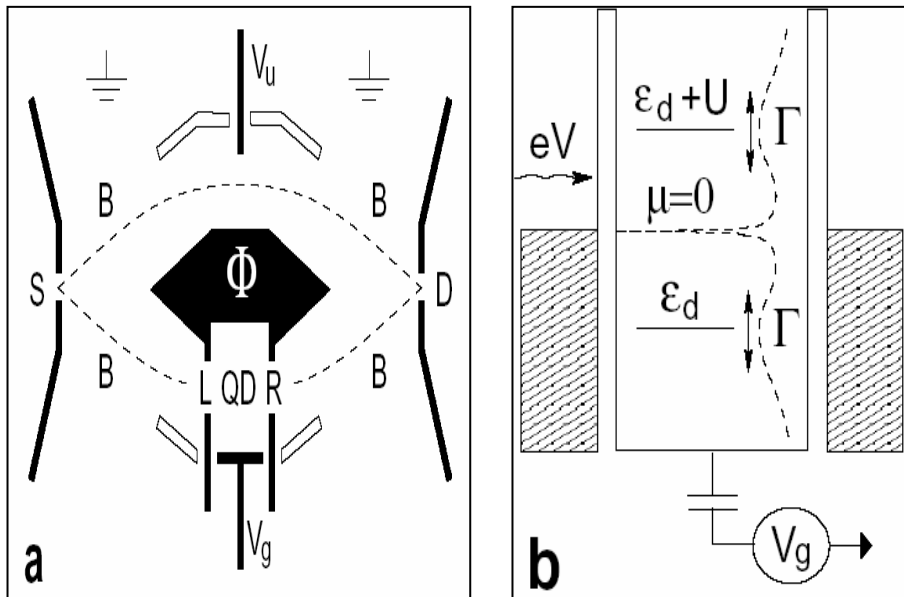


Experiment

(Ji, Heiblum et al.
Science **290** 779 (2000))

Theory-Experiment ballgame

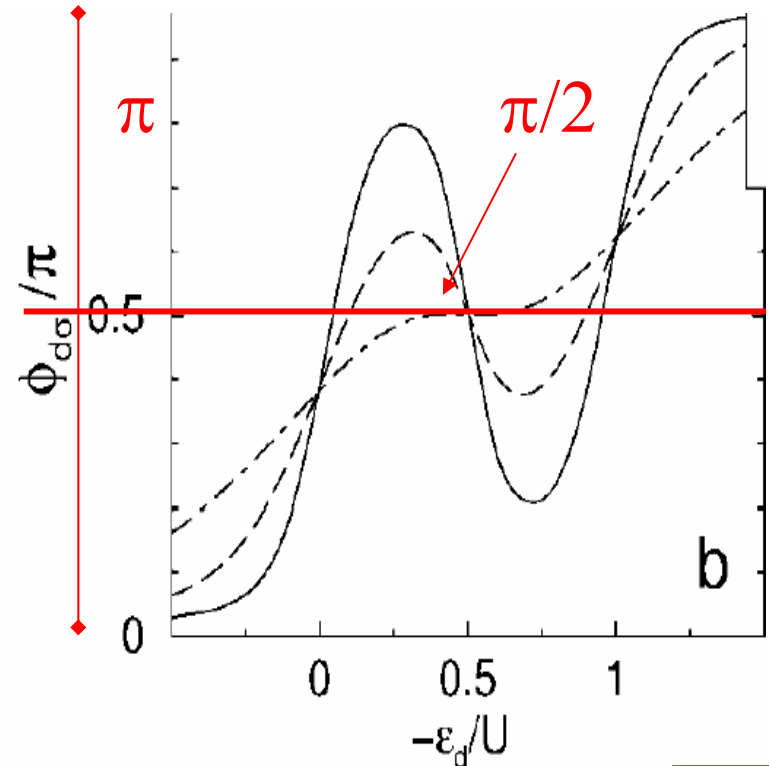
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Theory

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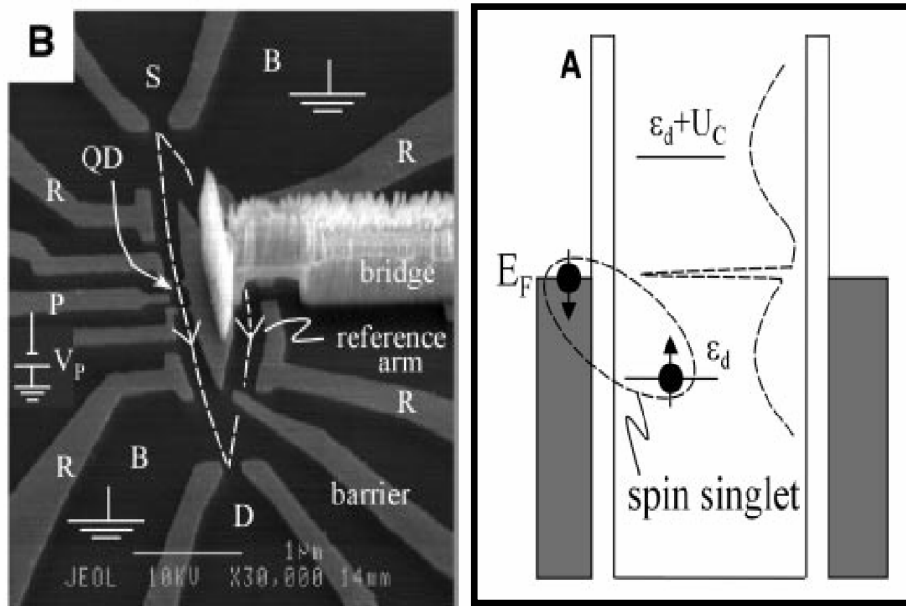


(c) For arbitrary temperatures ($\lesssim \Gamma$), the only approach which gives reliable results for $G_{d\sigma}(E)$ for all Γ, U, ϵ_d is the numerical renormalization group (NRG)

Theory (Gerland et al. PRL **84** 3710 (2000))

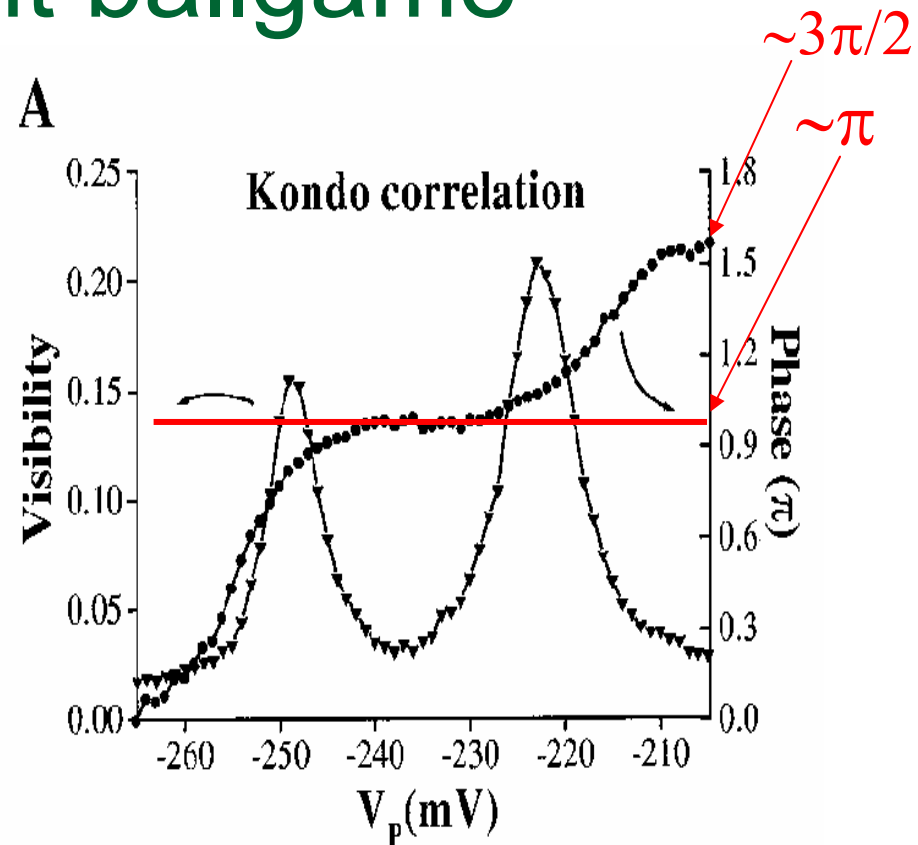
Theory-Experiment ballgame

Phase Evolution in a Kondo-Correlated System



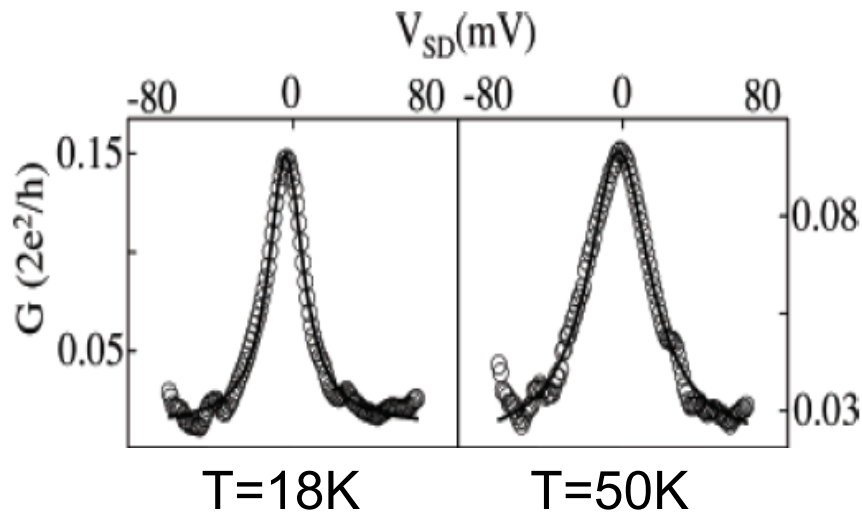
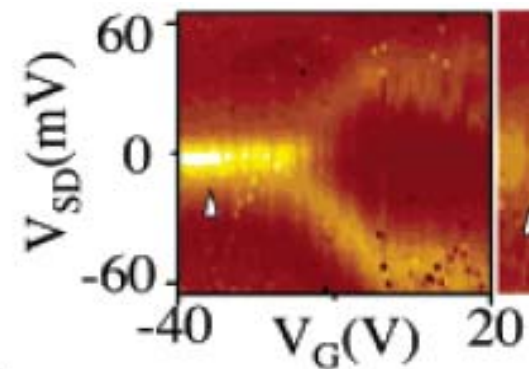
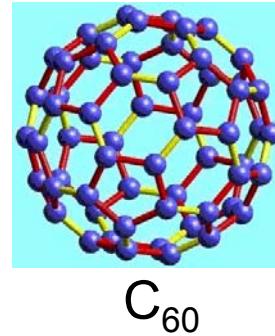
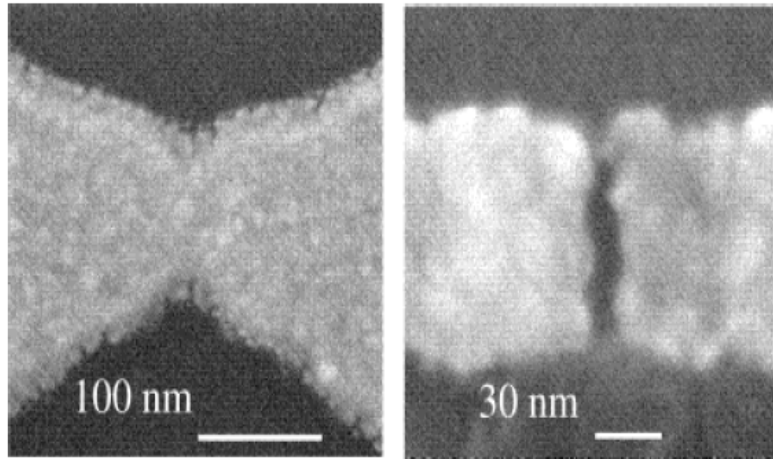
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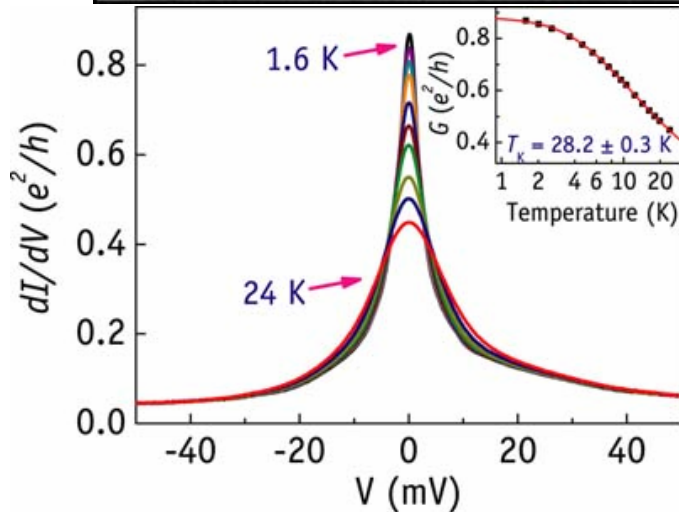
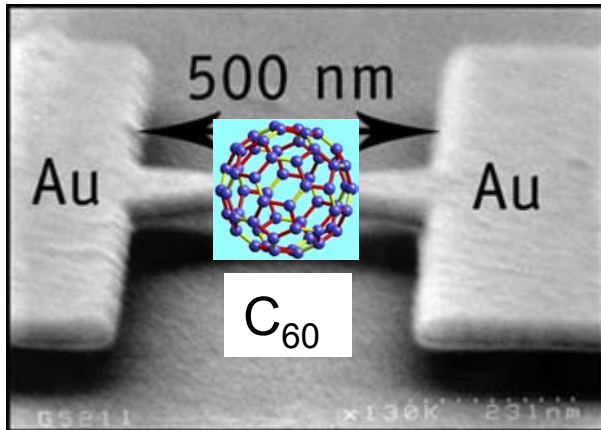
Experiment (Ji et al. *Science* **290** 779 (2000))

Kondo effect in Single Molecule Transistors

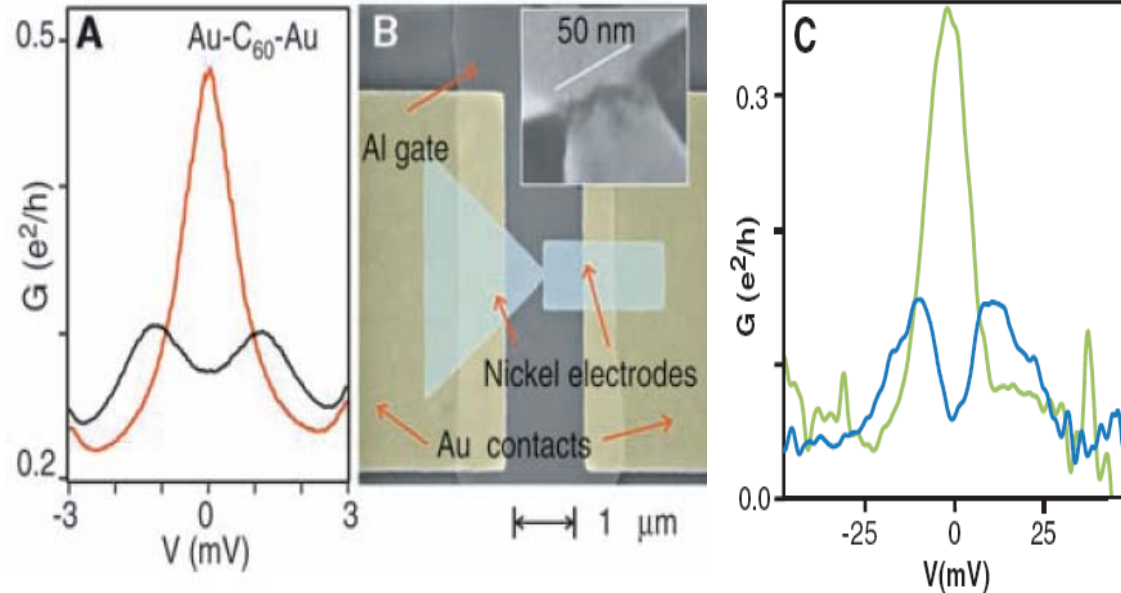


- Single molecule transistors: C_{60} molecules “caught” between electrodes (break junction).
- Zero-bias peak as a function of gate voltage: correct Kondo scaling.
- Correct behavior vs. Bias.
- $T_K > 50K$.

Kondo effect in Single Molecule Transistors



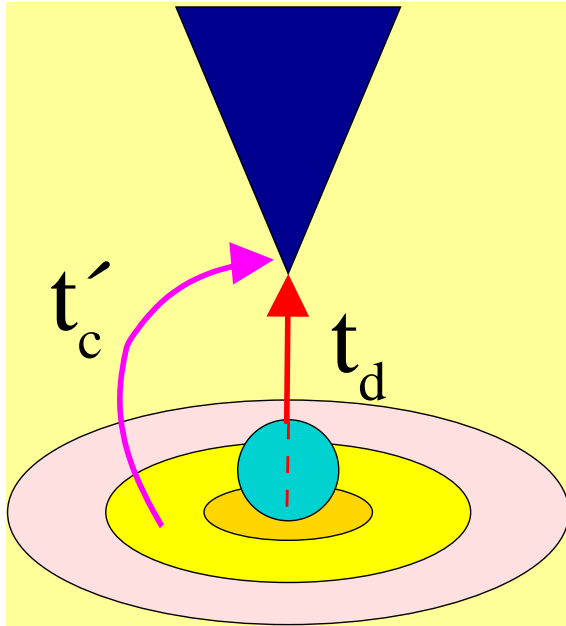
Pasupathy et al., *Science* **306** 86 (2004)



- Similar expts (D. Ralph's group).
- Suppression of the Kondo resonance in the presence of a **magnetic field** (top left, black curve, $B=10\text{T}$) and **magnetic leads** (top right, parallel [green] and antiparallel [blue] magnetizations).

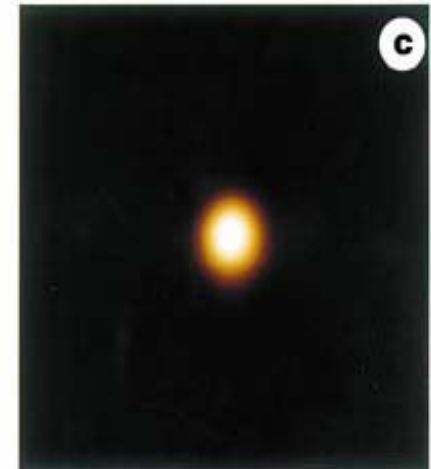
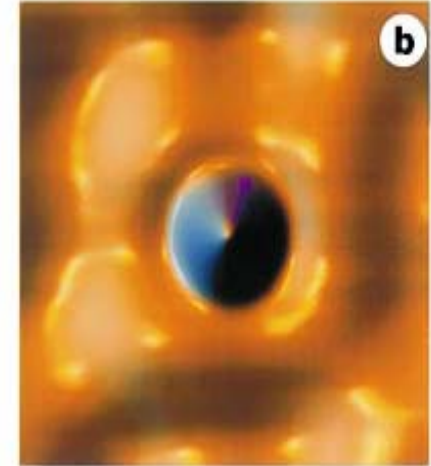
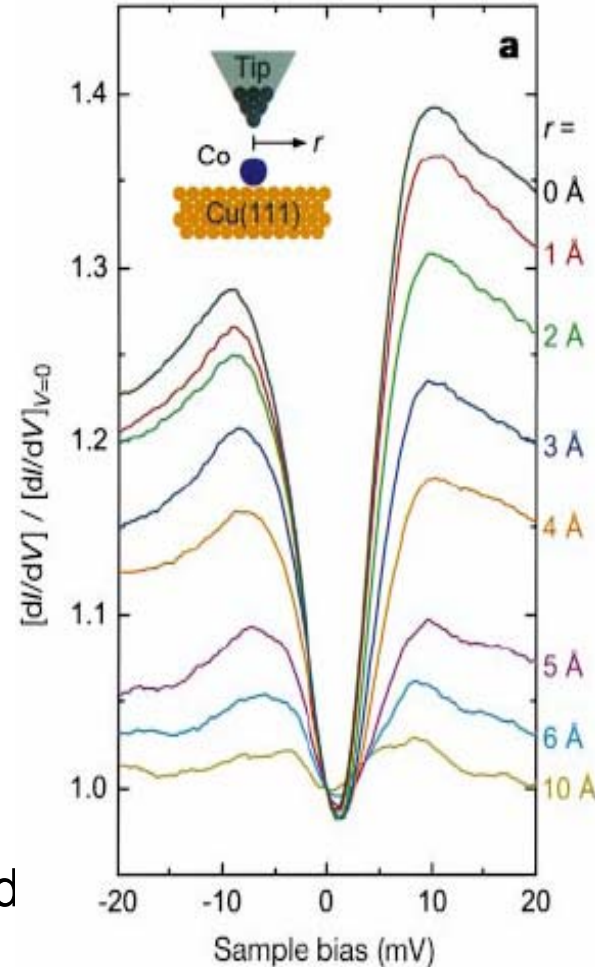
From Dan Ralph's webpage:
<http://people.ccmr.cornell.edu/~ralph/>

Kondo effect in surfaces (STM images).

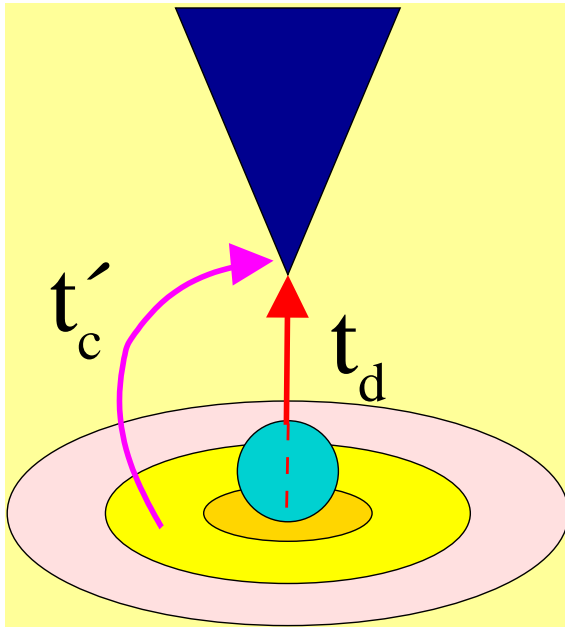


- Magnetic (Co, Fe) atoms on metallic *surfaces*! Right ingredients for Kondo.
- In this case, Kondo is marked by a *dip* at zero-bias conductance (dI/dV at $V=0$).

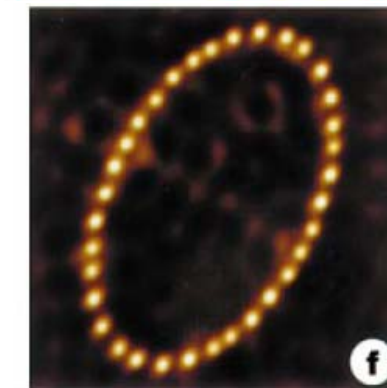
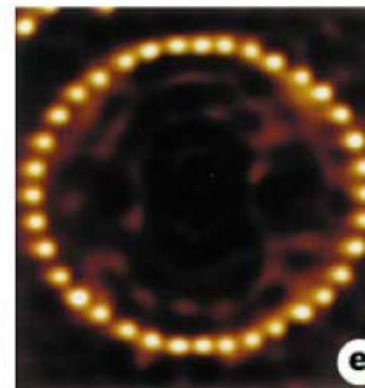
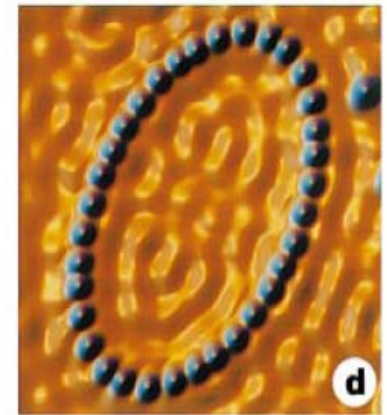
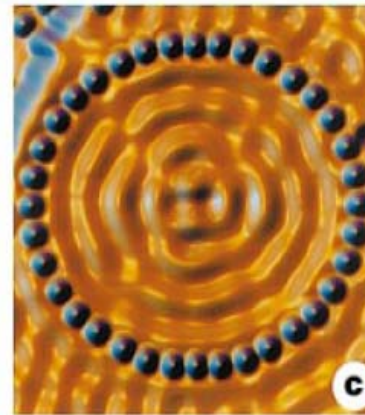
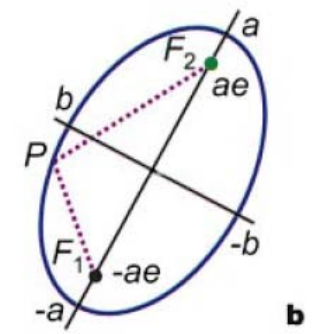
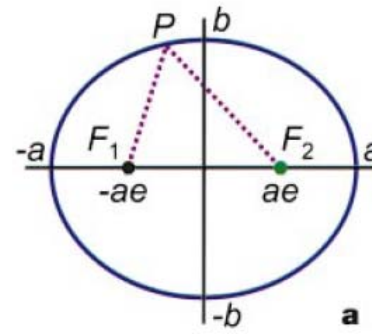
Manoharan et al., *Nature* **403** 512 (2000).



Kondo effect surfaces: STM measurements.

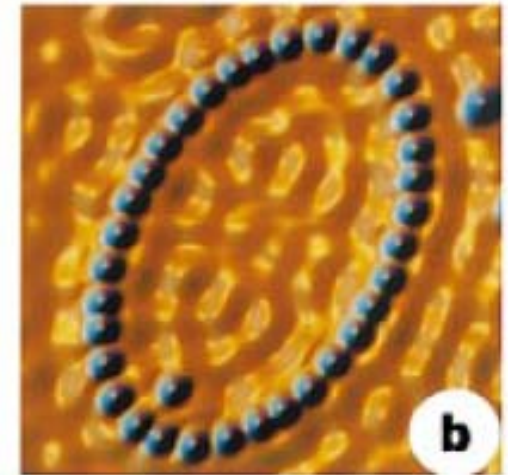
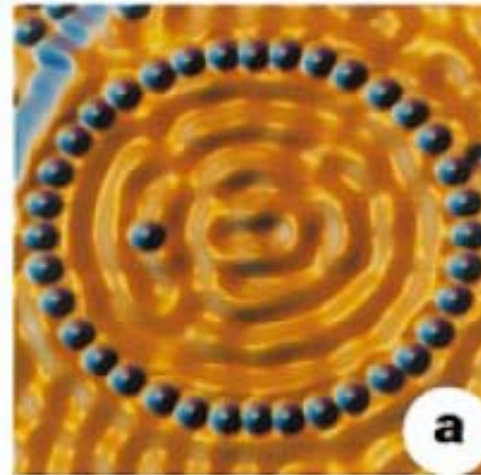
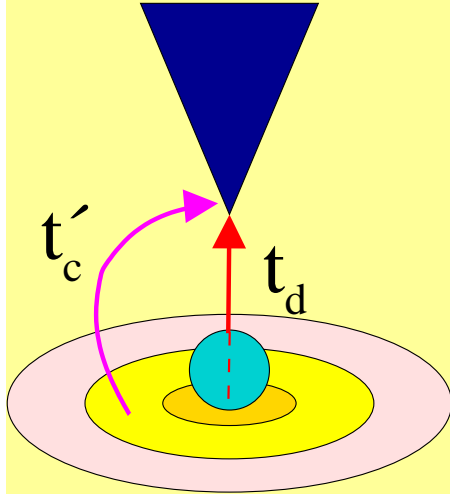


- STM atomic manipulation: can build local structures (“quantum corrals”).
- Elliptical shape: **imaging** (top) and **dI/dV** measurements (bottom).
- Cobalt atoms on Cu(111) shown.

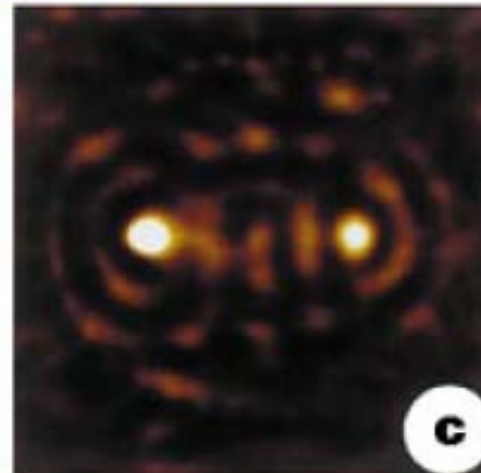


Kondo effect surfaces: STM measurements.

Manoharan et al., *Nature* **403** 512 (2000).

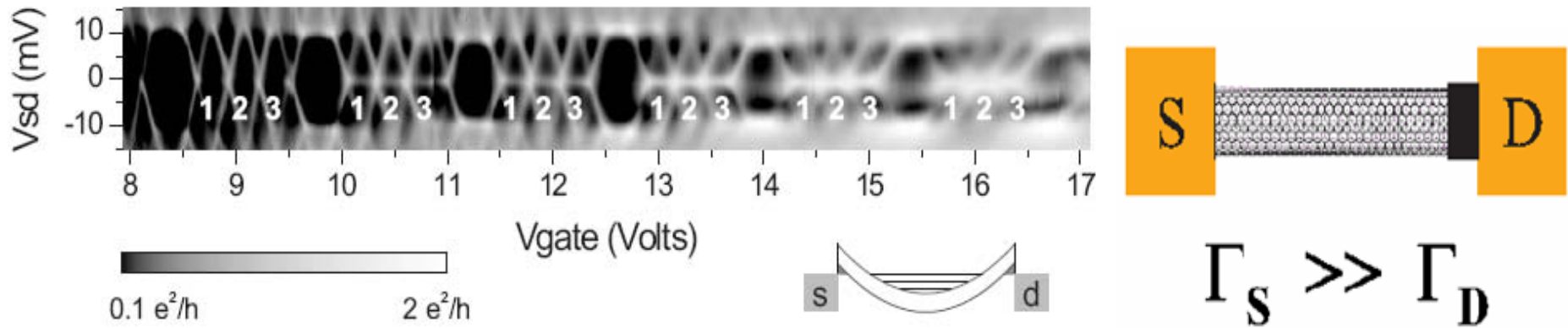


- One extra atom placed in one foci: a **peak in the dI/dV** appears in the other focus although **NO ATOM** is there! (“quantum mirage”).
- Theory: “focusing” of Kondo-scattered surface electrons*.



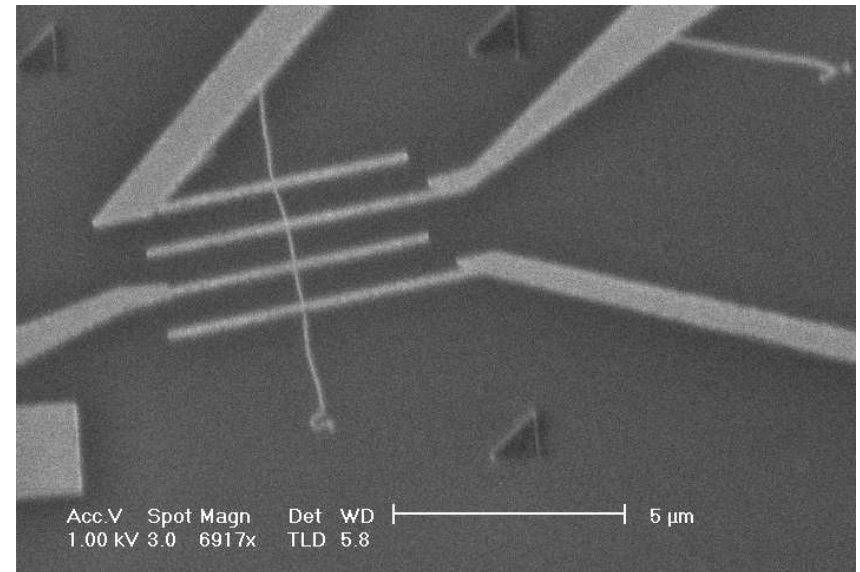
*Schiller and Agam, *PRL* **86** 484 (2001)..

Kondo effect In Carbon nanotubes.

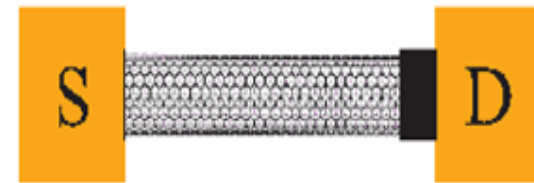
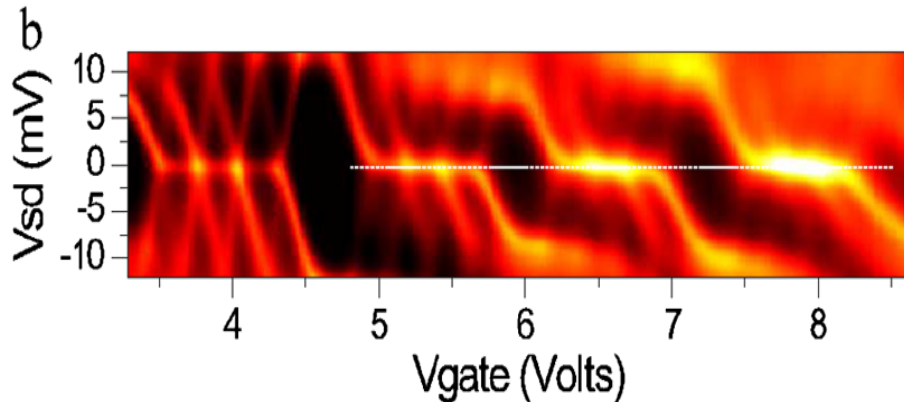


Makarovski, Zhukov, Liu, Filkenstein *PRB* **75** 241407R (2007).

- Carbon nanotubes deposited on top of metallic electrodes.
- Quantum dots defined *within* the carbon nanotubes.
- More structure than in quantum dots: “shell structure” due to *orbital* degeneracy.

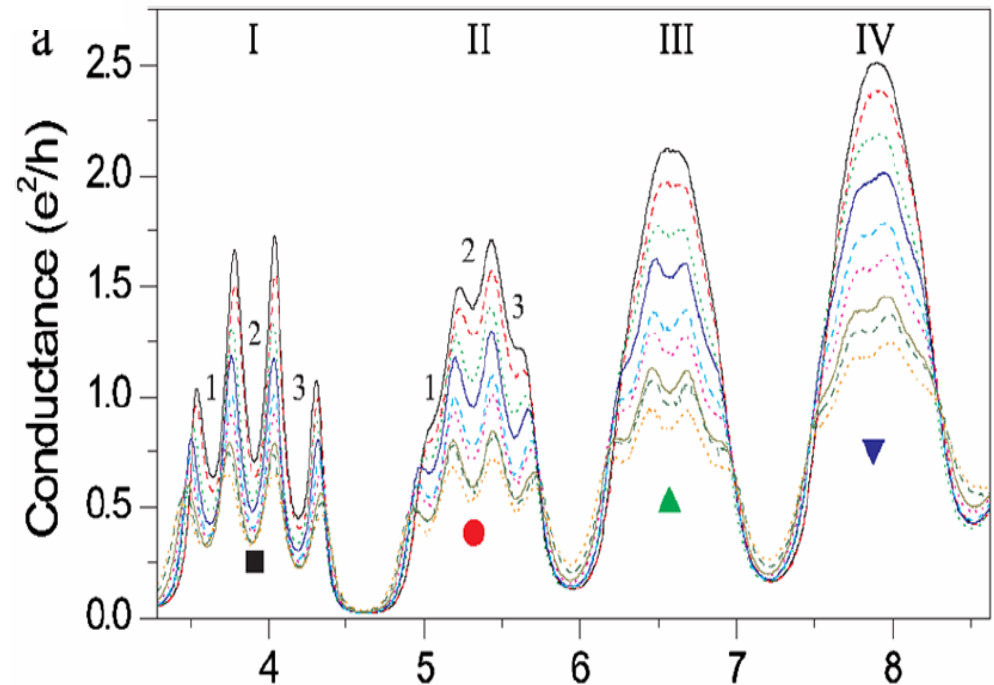


Kondo effect In Carbon nanotubes.



$$\Gamma_S \gg \Gamma_D$$

- Temperature behavior is Kondo-like.
- Interesting *merging of the four shells* at high V_g (“SU(4)” Kondo instead of the usual SU(2) Kondo).
- NRG calculations* support that picture.



Makarovski, Liu, Filkenstein *PRL* **99** 066801 (2007).

* Anders, Logan, Galpin, Filkenstein *PRL* **100** 086809 (2008).