First-principles study of the low-temperature charge density wave phase in the quasi-one-dimensional Weyl chiral compound (TaSe₄)₂I

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Using ab initio density functional theory, we study the lattice phase transition of quasi-one-dimensional (TaSe₄)₂I. In the undistorted state, the strongly anisotropic semimetal band structure presents two nonequivalent Weyl points. In previous efforts, two possible Ta-tetramerization patterns were proposed to be associated with the low-temperature structure. Our phonon calculations indicate that the orthorhombic F222 CDW-I phase is the most likely ground state for this quasi-one-dimensional system. In addition, the monoclinic C2 CDW-II phase may also be stable according to the phonon dispersion spectrum. Since these two phases have very similar energies in our density functional theory calculations, both these Ta-tetramerization distortions likely compete or coexist at low temperatures. The semimetal-to-insulator transition is induced by a Fermi-surface-driven instability that supports the Peierls scenario, which affects the Weyl physics developed above TCDW. Furthermore, the spin-orbit coupling generates Rashba-like band splittings in the insulating charge density wave phases.

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I. INTRODUCTION

One-dimensional (1D) systems continue to attract considerable attention due to their rich physical properties and reduced dimensional phase space. In particular, in low-dimensional systems the electron-electron, phonon-phonon, electron-phonon, and spin-phonon couplings are strongly enhanced by the interactions between transition-metal ions [1,2]. Under some conditions, free carriers may form charge density wave (CDW) or spin density wave (SDW) states due to the partial or complete condensation of excitations, properties which are physically interesting and important for possible applications [3–5].

Several 1D bulk compounds have been widely studied. For example, with a focus on the electronic correlation effects, the Cu-oxide 1D ladders were theoretically predicted and experimentally confirmed to have a spin gap and become superconducting [6–9]. Recently, an analogous behavior was shown to develop in iron ladders BaFe₂X₃ (X = S or Se) that were reported to be superconducting at high pressure [10–14]. By considering phononic modes or spin-phonon instability, ferroelectric or multiferroelectric states were predicted in some 1D systems [15–20]. (TaSe₄)₂I is a typical paradigmatic quasi-1D material that has been frequently studied for more than 30 years [21,22]. This system undergoes a Peierls phase transition at 263 K, the so-called CDW transition, accompanied by an incommensurate structural distortion at low temperatures [23–25]. Above the critical temperature TCDW = 263 K, the nearest-neighbor (NN) Ta-Ta distances (dTa-Ta = 3.206 Å at room temperature [22,26]) are identical along each chain. As expected, the CDW instability breaks the symmetry of the isometric chains leading to Ta-tetramerization modes [25–27]. Related experiments revealed that the Ta-tetramerization periodicity may be c = 4dTa-Ta [24,25,28,29]. In addition, this system is also considered to be a Weyl semimetal [30,31]. More recently, possible axion physics was proposed for this special chiral Weyl material [32,33]. It also should be noted that Rashba-like band splittings may also occur in a chiral system [34]. Since the spin-orbit coupling (SOC) for Ta’s 5d orbitals can be robust, such Rashba splitting is expected. All these developments in (TaSe₄)₂I provide a unique and promising platform to display different interesting physical properties in a single material.

In previous works, two Ta-tetramerization patterns were proposed for the low-temperature structure, corresponding to the 1D B₁ and B₂ representations [26]. Since the Ta-tetramerization distortion is small, it can only be observed via weak reflections, and for this reason the lattice phase transition is still uncertain. For this reason, from the theoretical perspective ab initio phonon calculations for the superstructure could play an important role in clarifying the real mechanism of lattice structural transition in this compound.

In the present publication, we perform first-principles density functional theory (DFT) calculations for (TaSe₄)₂I. First, our theoretical results indicate a strongly anisotropic electronic structure for the undistorted phase, corresponding to its quasi-1D geometry. Based on phononic dispersion calculations, we found that (TaSe₄)₂I contains phonon softening instabilities in the Γ₄ mode, resulting in an orthorhombic distortion, which could correspond to the B₁ or B₂ representation. By considering the combined B₁ + B₂ symmetry breaking,
The system would decrease to the monoclinic C2 phase (No. 5) with a pattern along chains involving four different NN Ta-Ta distances. Our DFT calculations suggest that the CDW-I lattice phase is the most likely ground state for this system. Since the energy difference between the two CDW lattices, B1 and B2, cannot be distinguished unambiguously, these two Ta-tetramerization phases are competitive at low temperatures. Our results also support that the semimetal-insulator transition is driven by the Fermi surface instability. Furthermore, for the heavy element Ta, moderate Rashba-like splitting bands are found in the low-temperature CDW phases.

**II. METHODS AND MODEL SYSTEM**

In this publication, DFT calculations were performed using projector augmented wave (PAW) pseudopotentials with the Perdew-Burke-Ernzerhof format revised for solid exchange functional (PBEsol), as implemented in the Vienna Ab initio Simulation Package (VASP) code [35–38]. The phonon spectra were calculated using the finite displacement approach and analyzed by the PHONOPY software [39,40]. Details are reported in the Supplemental Material [41].

Under ambient conditions, (TaSe4)2I forms a quasi-1D body-centered tetragonal chiral crystal structure with space group 1422 (No. 97). The lattice parameters are a = 9.531 Å and c = 12.824 Å [22]. There are two adjacent TaSe4 chains along the c axis in the conventional cell, where iodine atoms are located between chains, as shown in Fig. 1(a). In each TaSe4 chain, the Ta atoms are aligned equidistantly and the Se atoms form a “screw” arrangement along the c axis [see Fig. 1(b)]. Previous experimental results suggested that the modulated structure of (TaSe4)2I can be split into two parts [26] below the transition temperature TCDW = 263 K.

Since the equal displacements of all atoms would not change the space-group symmetry, we focus on the modulation of the Ta-tetramerized atoms, which corresponds to the parallel component of the qf vector (qfCDW) along the Ta-chain direction. By considering the space-group symmetry 1422 (No. 97), the Ta atoms occupy two different Wyckoff sites (4c and 4d). Based on the Raman active modes analysis [42], the corresponding Raman active modes of the 4c and 4d sites have B2 and B1 symmetry, respectively. Since the CDW instability corresponds to the Ta-tetramerization modes [25,26], a long-long-short-short (LLSS) Ta-tetramerization CDW-I pattern is expected by only considering the lattice dynamical B1 or B2 Ta tetramerization, as shown in Fig. 1(c) [43]. If, instead, we consider the combined B1 + B2 Ta tetramerization, there would be four different NN Ta-Ta distances in the chain [see Fig. 1(d)]. Based on the symmetry analysis, those two CDW phases corresponding to two Ta-tetramerization patterns are the most likely low-temperature structure. In addition, to better understand the Ta-tetramerization pattern along the chain direction, we calculated the phonon dispersion spectrum of a 1 × 1 × 4 supercell for the parent phase based on the conventional cell. We only found that an unstable Γ4 mode appears at Γ (see Fig. S1 in the Supplemental Material [41]), resulting in the LLSS Ta-tetramerization (CDW-I phase). Hence, we only consider these two states here. In addition, the AMPLIMODES software was employed to perform a group theoretical analysis [44,45], indicating that the CDW-I phase would induce an orthorhombic distortion from the undistorted tetragonal phase with phonon mode Γ4. The same analysis for the CDW-II phase also indicates that a monoclinic distortion is obtained, with phonon modes Γ5 and Γ4 corresponding to the undistorted tetragonal phase and the CDW-I orthorhombic phase, respectively.

**III. NON-CDW PHASE**

Before discussing the CDW phase, we consider the electronic structure corresponding to the non-CDW phase of (TaSe4)2I, which is displayed in Fig. 2. Here, we use the primitive cell instead of the conventional cell to calculate the electronic structure of (TaSe4)2I. The volume of the primitive cell is half that of the conventional cell with the primitive lattice: a1 = (−a/2, a/2, c/2), a2 = (a/2, a/2, −c/2), and a3 = (a/2, a/2, −c/2), where a and c are the conventional cell-lattice constants.

First, we present the band structure of the undistorted phase of (TaSe4)2I without the SOC effect. This band structure clearly displays strong anisotropic metallic behavior, as presented in Fig. 2(a). The band is more dispersive from Γ to Z along the chains than along other directions (i.e., N to P), which is compatible with the presence of quasi-1D chains along the k1 axis. As shown in Fig. 2(a), the Fermi level is dominated by the Ta d5z2−r2 orbital along the chains, in agreement with previous studies [25,27]. The crossing point along the chain direction (Γ to Z) is not at π/c but at the incommensurate kF where 2kF = qfCDW.

Next, we introduce the SOC effect to the undistorted state and now the bands begin to split as displayed in Fig. 2(b), which is consistent with other results [30,31]. In principle, as suggested by the band structure, (TaSe4)2I should also display two interesting Weyl points, with one along the Γ-to-Z path and the other along the N-to-P path, although this aspect requires further detailed calculations and discussion beyond the scope of this publication. However, note that the Weyl physics of this compound has been studied in detail in recent publications [30,31]. For this reason, here we primarily focus on the phononic aspects.
IV. CDW INSTABILITY

It is well known that the CDW instability is accompanied by a structural atomic rearrangement, related to the phonon mode instability. To understand the structural phase transition in (TaSe$_4$)$_2$I, we performed phononic dispersion calculations for both the non-CDW and the CDW phases. Figure 3(a) indicates the phonon dispersion spectrum that presents an imaginary frequency appearing at $\Gamma$ for the undistorted structure. The Ta-tetramerization arising from this mode corresponds to the CDW-I phase. According to group theory analysis using the AMPLIMODES software [44,45], this spontaneous distortion mode is a $\Gamma_4$ mode resulting in a twice larger periodicity (4$d_{Ta-Ta}$) along the TaSe$_4$ chain [47]. In addition, the phonon softening mode also corresponds to the transverse component of the incommensurate CDW wave vector parallel to the chain direction ($\Gamma$ to $Z$), as in x-ray diffraction and ARPES data [26,29].

We fully relaxed the crystal lattice from the original tetragonal $I422$ phase along these mode displacements and then obtained an orthorhombic $F222$ state (No. 22). Based on the relaxed orthorhombic structure, we found the LLSS Ta-tetramerization configuration, with the difference between the long NN and the short NN Ta-Ta distances being about $\sim$0.083 Å. Furthermore, we also calculated the phonon dispersion spectrum for the orthorhombic $F222$ phase (No. 22), and in this case no imaginary frequency mode was found, as shown in Fig. 3(b). By extracting the lowest-energy phonon mode of the orthorhombic $F222$ phase and applying it to the $F222$ phase, the symmetry of the crystal structure further decreases to the monoclinic $C2$ phase (No. 5) with a pattern of four different NN Ta-Ta distances along the chain, corresponding to the $B_1 + B_2$ representations. The AMPLIMODES software [44,45] indicates that this is the $\Gamma_4$ mode distortion for the orthorhombic $F222$ phase. After full lattice relaxations for the monoclinic $C2$ phase (No. 5), we find that the differences in the two long versus short Ta-Ta distances are 0.003 and 0.002 Å, respectively. Figure 3(c) indicates that the monoclinic CDW-II phase is also dynamically stable because no imaginary frequency mode is obtained in the phonon dispersion calculation. Here, it should be noted that the difference in energies of the orthorhombic versus monoclinic cases is quite small ($\sim$0.1 meV/Ta), beyond the accuracy of DFT. In this context, then, these two phases cannot be distinguished by considering such a small monoclinic distortion and almost-negligible energy difference. Additional DFT results for these two phases can be found in the Supplemental Material [41].

Next, let us focus on the semimetal-to-insulator transition. It is well known that there is a very small overlap between the bottom of the conduction band and the top of the valence band in the semimetallic material, resulting in a negligible density of states (DOS) without SOC at the Fermi level, as shown in Fig. 4(a). The DOS of the undistorted phase (No. 97) is presented in Fig. 4(b), indicating a semimetal with indeed quite a low density at the Fermi level. Furthermore, we also present in Figs. 4(c) and 4(d) the DOS for the distorted CDW phases.
(a) Schematic of the DOS semimetal-to-insulator transition. (b–d) DOS (without SOC) near the Fermi level for the undistorted parent (non-CDW), orthorhombic (CDW-I), and monoclinic (CDW-II) phases, respectively. Black, total; red, Ta; blue, I; green, Se.

showing that a gap opens in this case. By considering the SOC effect, the expected gap becomes approximately 0.2 eV at the crossing point along $\Gamma$ to Z corresponding to the Brillouin path of undistorted phases. Here, the Ta-tetramerization plays a key role in understanding the mechanism of the phase transition, which may be described by the Brillouin-zone center Peierls instability. As shown in Fig. 2, this system displays a quasi-1D band dispersion. Along the $P-X$ path, parallel to the chains, the two Ta $d_{3z^2}$ bands are separated at the $P$ point above the Fermi level with a small gap ($\sim 40$ meV), resulting in a narrow hole pocket. Along the $\Gamma-Z$ path, the two bands cross below the Fermi level, yielding a flat electron pocket. The pair is nested by the CDW parallel vector $q_{\text{CDW}}^{||}$, consistent with the Peierls scenario. Hence, our results are in agreement with the physical picture of a Fermi-surface-driven instability resulting in the Peierls transition. Furthermore, strictly speaking the two Weyl points disappear in the low-temperature CDW phases due to the opening of a gap. This suggests that Weyl physics could be altered below $T_{\text{CDW}}$. Because the phase transition seems to be of first order, as suggested by neutron scattering studies [26], the physics below and above $T_{\text{CDW}}$ could be qualitatively different with regard to the Weyl features.

Then we briefly discuss the impact of doping effects in this system. Usually, for strong electron-phonon coupling CDW systems, a dilute isoelectronic doping should have little effect on the CDW transition temperature and CDW state because the location of the carriers is determined by the electron-phonon coupling [48]. However, in contrast to other CDW systems, a surprising change in the modulation wave vector was reported in Nb-doped (TaSe$_4$)$_2$I, where a dramatic dependence of the satellite position was found at a low doping concentration 1% [49]. For nonisoelectronic doping, the doping effect can be described by the rigid-band picture where the conduction electron density is directly dependent on the dopant ion concentration.

To understand better the lattice phase transition, we simulated the switching “path” from the undistorted phase (no Ta-tetramerization) to the CDW-I LLSS Ta-tetramerization phase by a simple linear interpolation of the $\Gamma_4$ mode, as shown in Fig. 5(a). The transition energy wall between the two phases was computed to be $\approx 40$ meV/Ta. However, note that we fixed the crystal constants to obtain the switching path and this would increase the energy barrier. In addition, we also compare the switching path between the CDW-I and the CDW-II phases and here the energy wall is much smaller, $\approx 0.4$ meV/Ta [see Fig. 5(b)], which corresponds to a small monoclinic distortion.

V. ADDITIONAL DISCUSSION

The point groups of (TaSe$_4$)$_2$I for the undistorted (space group No. 97), CDW-I (space group No. 22), and CDW-II (space group No. 5) phases are $D_4$, $D_2$, and $D_2$, respectively.
For the monoclinic C2(C2)2 CDW-I phase. (b, d) For the orthorhombic point in the bulk Brillouin zone are obtained from the Seek-path software [46]. (a, c) For the orthorhombic P 222 CDW-I phase. (b, d) For the monoclinic C2 CDW-II phase.

2 (C2), respectively. In all these cases, optical isomerism is allowed in this quasi-1D system. For this reason, optical activity effects are expected by considering their chiral point group. We thus suggest that further experimental and theoretical works should focus on the optical isomerism of this material.

Furthermore, for the heavy element Ta, the SOC for the 5d orbitals is expected to be large enough to induce a band splitting. Since the point groups of (TaSe4)2I for both the non-CDW and the CDW phases are the noncentrosymmetric chiral group, a Rashba-like band splitting is also expected in this system. We calculated the band structures for the two CDW phases with SOC incorporated, with the results shown in Fig. 6. There it is shown that the split bands resemble Rashba splitting along the high-symmetry directions, as shown in Figs. 6(a) and 6(b). Moreover, we also show the bands of CDW-I phases near the Γ and T points that indicate a clear Rashba-like band splitting, as in Fig. 6(c). Similar Rashba-like band splittings [see Fig. 6(d)] indicate that these effects can also occur in the CDW-II phase. This is also reasonable since the monoclinic distortion is too small to completely alter the dominant physical properties. In fact, Rashba-like bands also develop along the Γ-to-Z and N-to-P paths in the non-CDW parent phase. These issues deserve further studies in the future. It also should be noted that Shi et al. [30] found that the CDW couples the momentum-separated Weyl points with opposite chiral charge, providing a venue for the examination of topological insulating phases.

VI. CONCLUSIONS

In summary, here the quasi-1D compound (TaSe4)2I has been systematically studied using first-principles calculations. A strongly anisotropic metallic band structure was observed in the undistorted Weyl phase (non-CDW state), in agreement with previous experimental and theoretical works. In addition, using the group symmetry analysis and DFT calculations, two Ta-tetramerization CDW phases have been found here to become the stable low-temperature structure. The semimetal-to-insulator transition is induced by the Fermi-surface-driven instability, resulting in a Peierls transition that opens a gap (∼0.2 eV). In addition, based on the linear interpolation of the Γ4 mode, the transition energy barrier is estimated to be ≈ 40 meV, corresponding to a high transition temperature. Furthermore, for the heavy element Ta, the spin-orbit coupling for its 5d orbitals should be robust, causing a delicate but noticeable Rashba splitting of the conducting bands around the Γ point in this polar system (chiral). Our results successfully reproduce the phase transition induced by the CDW instability and provide additional insight that may motivate further theoretical and experimental efforts. In future work we will explore the possibility of Rashba effects in these low-dimensional chiral materials.

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[40] For more results, see Supplemental Material at http://link.aps.org/supplemental/10.1103/PhysRevB.101.174106 which is associated with this publication.
[42] The two Ta sites (4c and 4d) form the pattern Ta(1)-Ta(2)-Ta(1)-Ta(2) in the chain direction. In the B\textsubscript{1} representation, two Ta(1) atoms (4c site) move towards the connected Ta(2) atoms in chain A and move away from the connected Ta(2) atoms in chain B, resulting in an LLSS Ta-tetramerization pattern. Correspondingly, in the B\textsubscript{2} representation, the Ta(2) atoms (4d site) move towards the connected Ta(1) atoms in chain A and move away from the connected Ta(1) atoms in chain B. Both the B\textsubscript{1} and the B\textsubscript{2} representations would induce a similar LLSS Ta-tetramerization CDW phase, as shown in Fig. 1(c).
[46] Here, for completeness we also used 1 × 1 × 2 and 1 × 1 × 4 supercells based on the conventional cell, but none of our physical conclusions changed, as shown in the Supplemental Material [41].