Problem 2:

Using the expressions provided in class we find

$$\mathbf{a}_{1}' = \frac{4\pi}{d} \frac{1}{2} (\hat{\mathbf{y}} + \hat{\mathbf{z}} - \hat{\mathbf{x}}),\tag{1}$$

$$\mathbf{a}_2' = \frac{4\pi}{d} \frac{1}{2} (\hat{\mathbf{z}} + \hat{\mathbf{x}} - \hat{\mathbf{y}}), \tag{2}$$

$$\mathbf{a}_{3}' = \frac{4\pi}{d} \frac{1}{2} (-\hat{\mathbf{x}} + \hat{\mathbf{y}} + \hat{\mathbf{z}}). \tag{3}$$

These three vectors expand a body centered cubic lattice. The side of the cubes in the reciprocal lattice have length $\frac{4\pi}{d}$ where d is the length of the cubes in the original fcc lattice.