

Homework #7

Problem 1:

$$F^{\alpha\beta} = \begin{pmatrix} 0 & -E_x & -E_y & -E_z \\ E_x & 0 & -B_z & B_y \\ E_y & B_z & 0 & -B_x \\ E_z & -B_y & B_x & 0 \end{pmatrix}$$

$$F_{\alpha\beta} = \begin{pmatrix} 0 & E_x & E_y & E_z \\ -E_x & 0 & -B_z & B_y \\ -E_y & B_z & 0 & -B_x \\ -E_z & -B_y & B_x & 0 \end{pmatrix}$$

$$F^{\alpha\beta} F_{\alpha\beta} = 2(B^2 - E^2)$$

$$\mathcal{F}^{\alpha\beta} = \begin{pmatrix} 0 & -B_x & -B_y & -B_z \\ B_x & 0 & E_z & -E_y \\ B_y & -E_z & 0 & E_x \\ B_z & E_y & -E_x & 0 \end{pmatrix}$$

$$\mathcal{F}_{\alpha\beta} = \begin{pmatrix} 0 & B_x & B_y & B_z \\ -B_x & 0 & E_z & -E_y \\ -B_y & -E_z & 0 & E_x \\ -B_z & E_y & -E_x & 0 \end{pmatrix}$$

$$\mathcal{F}^{\alpha\beta} F_{\alpha\beta} = -4\vec{E} \cdot \vec{B}$$

$$\mathcal{F}^{\alpha\beta} \mathcal{F}_{\alpha\beta} = 2(E^2 - B^2)$$

$$F^{\alpha\beta} \mathcal{F}_{\alpha\beta} = -4\vec{E} \cdot \vec{B}$$